

How does electric current flow?
How can current, voltage and resistanc
How can electricity become useful to us
How can the cost of electricity be calcul
How can electricity be conserved?
•

om the mathematical point of the view:
-multiply,
-divide,
-use fractions and composite numbers,
-use cancelation rule, identify and solve exponential functions (with the base n while naming metric multipliers,
-solve linear equations with one variab unknown variables,
-plot and read graphs and interpret bill
redict which substances are conductors,
esign series and parallel circuits and lea start the flow of current.
ake informed decisions before buying b bulbs for home or special projects.
e aware of electrical usage and find way money.
lake conscious changes in habits or lifes 1y.
now how to live without electricity for sl

common nonlinear functions/relations.) • Approach and Reasoning-The strategies and skills used to solve the problem, and the reasoning that supports the approach; extensions, and generalizations; UNDERSTANDINGS: one after the other one

(another lesson).

through all of them -then the total Resistance "R" in Series circuits -but all partial resistors with R₁,R₂,R₃...R_n are in a line that can be "squeezed" into one point with still the same I and V through one of the parallel resistors thus the total Current is just the sum: the total Resistance I -further simplifying (by using the idea of reciprocals) we get the total Resistance: $R=1/(1/R_1+1/R_2+1/R_3+...+1/R_n)$

KNOWLEDGE:

now applied to our topic

57, in the resource1 #3) -safety precautions for electrical circuits & batteries (electrochemical cells converting stored chemical energy into electrical) are same magnitude and same polarities) resistance in Series circuits is summed up resistance in Parallel circuits is calculated sum of reciprocals) COMMON MISCONCEPTIONS: While revising the safety precautions during the -prior vocabulary irst part of the first classroom meeting, it is al to stress the common misconception at Voltage kills – Voltage does not kill at all it the Current it generates does. 0.1-0.2A is enough of I for an injury and 0.5A is usually Also, some students may try to memorize prrectly the total R as the sum of reciproca $_{1}+1/R_{2}+1/R_{3}+...+1/R_{n}$) because it look nore intuitive. It is important to tell the student hat they are almost right but that way they uld have calculated only 1/R. Explain t why the correct formula is *reciprocal sum* or *reciprocals* [$1/(1/R_1+1/R_2+1/R_3+...+1/R_n)$]

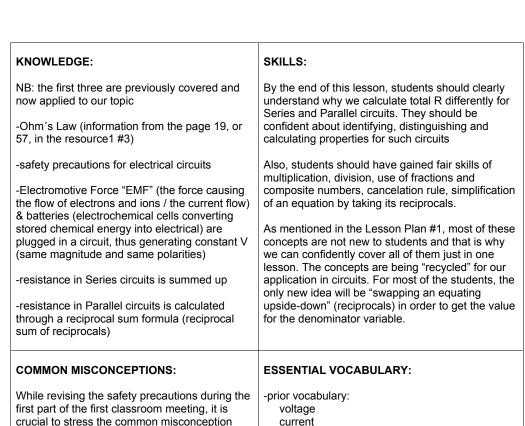
questions 1, 2, 14, 16, 18, 31, 36 on the resource2 #1 from relevant examples the same resource2 #1) their reasoning 20, 21, 30, 32 from the resource2 #1) concepts) **KEY CRITERIA:**

Lesson Plan: Mathematics behind Series & Parallel circuits, Reciprocals Grade Level: 9th Grade (Freshman High School), 1st semester **Context:** Electricity through Chemistry and Mathematics Estimated time: 4×80 minutes + consecutive 80 minutes long classroom meetings, the lesson is flexible and easy to be modified so that 8×40 minutes long sessions take place) BIG IDEA: After the students completely understood the Ohm's Law (including all - Electric urrent, Voltage, Resistance and Power) and they have been introduced to the electrical circu they should wonder what happens if they plug in more resistors in the same circuit. The students will understand why and how to calculate the total Resistance in different circuits in order to solve questions about different Ohm's Law relationships. That will be eventually applied to circuits with ore light bulbs plugged in and to their interchange that has impact on the total Power usage

STAGE ONE: DESIRED RESULTS **ESTABLISHED GOALS:** The students should leave the classroom with clear understanding of Series and Parallel circuits in relation to total resistance – i.e. their concepts, mathematical derivation and mathematical relationships of multiplication, division, squares and square roots and the idea behind reciprocals. The state standards of Vermont DoE are some previous (7.8.-20 & -21) with new ones that are more stressed throughout this lesson. All of them are listed below: • Standard 7.8: Functions and Algebra Concepts MHS: 19 Solves and models problems by formulating, extending, or generalizing linear and And makes connections among representations of functions/relations (equations, tables, graphs, symbolic MHS: 20 Demonstrates conceptual understanding of linear relationships and linear and nonlinear functions (including f(x) = ax2, f(x) = ax3, absolute value function, exponential growth) through analysis of intercepts, domain, range and constant and variable rates of change in mathematical and contextual MHS: 21 Demonstrates conceptual understanding of algebraic expressions by evaluating, simplifying, or writing algebraic expressions; and writes equivalent forms of algebraic expressions or formulas (d = rt—> r = d/t or solves a multivariable equation or formula for one variable in terms of the Standard 7.10: Mathematical Problem Solving and Reasoning—Applications MHS: 30 Demonstrate understanding of mathematical problem solving[2] and communication

• Execution-The answer and the mathematical work that supports it; • Observations and Extensions—Demonstration of observation, connections, application, • Mathematical Communication-The use of mathematical vocabulary and representation to communicate the solution; and • Presentation—Effective communication of how the problem was solved, and of the [2] Problem-solving situations are mathematical problems that reflect the levels of mathematic in the Grade Level Expectatio [4] See Vermont High School Level Mathematics Portfolio Scoring Guide for additional information. **ESSENTIAL QUESTIONS:** Series circuits have resistors lined up What are the different ways of combining more resistors in a circuit? -they have the same Voltage "V" (generated by How would we simplify them to a few basic kinds? a battery) and the same Current "I" flowing And how can the Current flow – what are the paths it can travel through? How would we try to calculate the total Resistance? And why would we want to do it i.e.: again, here the teacher should make it clear t the general application for this is wh electricians set up new circuits (e.g. building a -thence for R we sum up $(R=R_1+R_2+R_3+...+R_n)$ house); and at the same time, the teacher stress the fact that understanding of thi - Parallel circuits have resistors positioned crucial for further development in this unit (bul' parallel, one next to the other one interchanging) Ithough they have the same V, the I "flow" is What kind of a relationship from the Ohm's separated into independent ones, each going are we going to be looking at in order to actua V, R relationship, yet thinking without the

= $V/R_1+V/R_2+V/R_3+...+V/R_n$ = $\sqrt{(1/R_1+1/R_2+1/R_3+...+1/R_n)}$ = V×R where R is Is the Voltage same all through the circuit? Is the Current same all through the circuit? -but then we can divide ("cancel") both sides by V and we get $1/R=1/R_1+1/R_2+1/R_3+...+1/R_n$ If not, how is it split across all resistors (the same way or with a certain ratio)? How could we find a general expression for R?

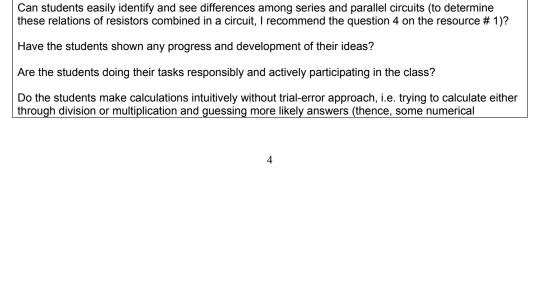


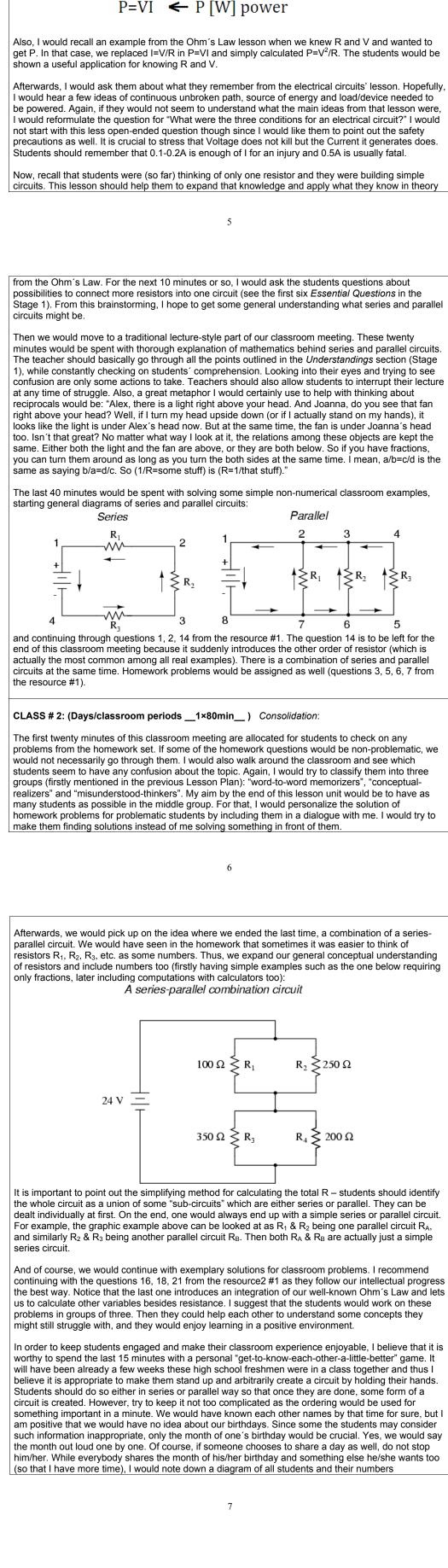
resistance, resistor . Ohm´s Law -circuits: series & parallel -sum & reciprocals

STAGE TWO: ASSESSMENT EVIDENCE PERFORMANCE TASK (S): (STUDENTS OTHER EVIDENCE: (FORMATIVE, SELF-ASSESSMENT STRATE BY SATISFACTORY igoing classroom evaluation based on student

olving classroom examples (e.g. some of the reactions, questions and answers -participation and reactions of students to tp://www.allaboutcircuits.com/pdf/worksheets/ | brainstorming discussion on the beginning of and classroom meeting (questions would be NB: the resource worksheet contains many example: "Do you think holiday lights are an good questions that are out of the knowledge for example of parallel or series bulbs in a circuit our class and therefore I selected only a few "Do you think the bulbs in the parallel circuit or the series circuit will burn brighter?", "If you remove a bulb in your parallel circuit, with the other bulb(s) -answering homework questions (e.g. some of still light?", "If you remove a bulb in your series the questions 3, 5, 6, 7, 13, 17, 19, 23, 37 on circuit, with the other bulb(s) still light?" – retrieved from the resource2 #2, page 8) -answering true false statements and providing | -students start the last (third) classroom meeting with a quick write up of the general R formula for Series and Parallel circuits (then, the teacher -calculating with reciprocals for both classroom would be able to quickly set back on track those work and homework (e.g. some of the questions | students who might be confused about the different

-participating in the final guiz requiring both -solving the homework problem created by the mathematical skills and contextual reading skills class itself on the end of the second classroom (again, see the resource2 #1 for the last and setting: students stand up and arbitrarily create a most comprehensive questions 38 and 40) circuit by holding their hands (either in series o parallel way) so that once they are done, everybody shares the month of his/her birthday that would actually represent the resistance value





examples should include numbers too big or too small – to uncommon – to be observed in the natural

Are the students able to solve more complex tasks such as the pointed questions from the resource2

a

STAGE THREE: LEARNING PLAN

(LESSON SEQUENCE + LEARNING ACTIVITIES, "WHERETO")

This lesson is placed towards the second half of our unit. Therefore, there has been a fair amount of

restate the questions for more specific ones, i.e. what are the signs and units for... After they would

also comment on the mathematical relationship among I, V, R, we would quickly do the same for the

[] A current

 $\mathbf{L} \ \mathbf{R} \left[\Omega \right] \ resistance$

nformation covered by this moment. Before starting to synthesize the ideas from the Ohm´s law

electrical circuits into one application, we would need to revise these main ideas. I would ask the

class what we know about current, voltage and resistance at first. As they would react promptly (hopefully), I would write a few notes on the blackboard. If nobody would respond, I would try to

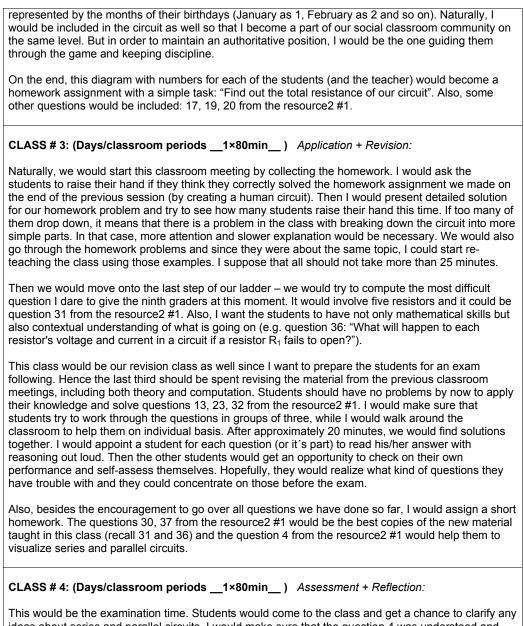
CLASS # 1: (Days/classroom periods __1×80min__) Prior knowledge + Introduction:

power as well. We should end up with something like this after a few (circa 5) minutes:

V=IR 🖌 V [V] volatage

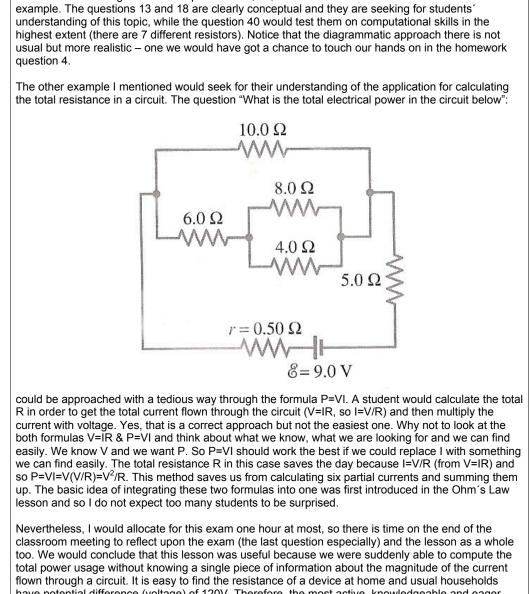
Do students have fun, enjoy the class and are they engaged?

#1 numbered 20+?

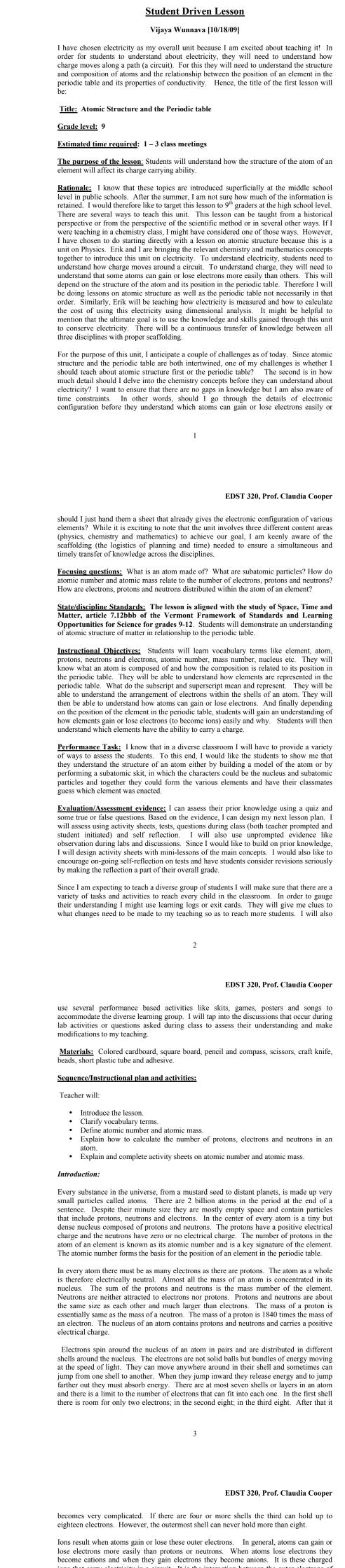


ideas about series and parallel circuits. I would make sure that the question 4 was understood and solved properly as I want to include a similar graphic approach on the exam.

e students would get to answer questions 13, 38, 40 from the resource2 #1 and one other



have potential difference (voltage) of 120V. Therefore, the most active, knowledgeable and eager students could be encouraged to calculate the power usage of some easily identifiable circuit at



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